ABSTRACT

This paper is to design PID controller to supervise and control the speed response of the DC motor and MATLAB program is used for industrial application. PID controllers are widely used in industrial plants because of their simplicity and robustness. The results obtained from simulation are approximately similar to that obtained by practical. Also the dynamic behavior is studied.

KEYWORDS: DC motor, PID controller, DC motor armature, DC motor speed response, MATLAB

I. INTRODUCTION

The DC motors have been popular in the industry control area for a long time, because there good characteristics, for example: high start torque characteristic, high response performance, easier to be linear control...etc. The speed of a DC motor is given by the relationship

\[ N = \frac{V - IaRa}{k\phi} \]  

where \( V \) is applied voltage, \( N \) is speed, \( Ia \) is armature current, \( Ra \) is armature resistance and \( \phi \) is the flux per pole[1].

This paper describes the MATLAB/SIMULINK of the DC motor speed control method namely field resistance, armature voltage, armature resistance control method and feedback control system for DC motor drives [2].

When speed control over a wide range is required, combination of armature voltage control and field flux control is used. This combination permits the ratio of maximum to minimum speed to be 20 to 50. With closed loop control, this range can be extended up to 200. The parameters of the PID controller \( kp, ki \) and \( kd \) can be manipulated to produce various response[3].

II. PID CONTROLLER:

The combination of proportional, integral and derivative control action is called PID control action. PID controllers are commonly used to regulate the time-domain behavior of many different types of dynamic plants. These controllers are extremely popular because they can usually provide good closed-loop response characteristics. Consider the feedback system architecture that is shown in Fig. 1 where it can be assumed that the plant is a DC motor whose speed must be accurately regulated [4].

![Feedback system of architecture](Fig 1 (a))

The PID controller is placed in the forward path, so that its output becomes the voltage applied to the motor’s armature the feedback signal is a velocity, measured by a tachometer. The output velocity signal \( C(t) \) is summed with a reference or command signal \( R(t) \) to form the error signal \( e(t) \). Finally, the error signal is the input to the PID controller.

\[ C(s) = K_p + \frac{K_i}{s} + K_ds = \frac{K_ds^2 + K_ps + K_i}{s} \]  

(2)
III. DC MOTOR MATHEMATICS MODEL AND THE CONTROL THEORY:

DC motors have speed-control capability, which means that speed, torque and even direction of rotation can be control at any time to meet new conditions [5]. The electric circuit of the armature and the free body diagram of the rotor are shown in the following fig-2 [6].

![Fig 2 electric circuit of dc motor](image)

Let \( R_a \) = Armature Resistance, \( L_a \) = Armature self inductance caused by armature flux, \( i_a \) = Armature current, \( i_f \) = field current, \( E_b \) = Back EMF in armature, \( V \) = Applied voltage, \( T \) = Torque developed by the motor, \( \theta \) = Angular displacement of the motor shaft, \( J \) = Equivalent moment of inertia of motor shaft & load referred to the motor, \( B \) = Equivalent Coefficient of friction of motor shaft & load referred to the motor. The DC motors are generally used in the linear range of the magnetization curve. Therefore, air gap flux \( \Phi \) is proportional of the field current i.e.

\[
\Phi \propto i_f
\]

\[
\Phi = K_f i_f
\]

where \( K_f \) constant

The torque \( T \) developed by motor is proportional to armature current and air gap flux

\[
T \propto i_a \Phi
\]

\[
T = K_f K_a i_a \Phi
\]

\[
T = K_t i_a
\]

where \( K_t \) is constant.

The motor back emf can be written as

\[
E_b \propto \omega \phi
\]

\[
E_b = K_b \omega
\]

\[
E_b = K_b \frac{d\phi}{dt} \quad (K_b \text{ is back emf constant})
\]

If we apply kcl on armature circuit

\[
v = R_a i_a + L_a \frac{di_a}{dt} + E_b
\]

The dynamic equation motor will be (\( J \) is moment of inertia \( B \) is coefficient of friction )

\[
T = J \frac{d^2 \theta}{dt^2} + B \frac{d\theta}{dt} + T_L
\]

Taking laplace transform of equation(8) (9) and (12).

\[
T(s) = K_I a(s)
\]

\[
E_b = K_b s \theta(s)
\]

\[
V(s) = I_a(s) (R_a + L_a s) + E_b
\]

\[
V(s) - E_b = I_a(s) (R_a + L_a s)
\]

and

\[
T(s) = (JS^2 + BS) \theta(s)
\]

\[
T(s) = (JS + B) s \theta(s)
\]

\[
T(s) = (JS + B) \omega(s)
\]

\[
T(s) = K_I a(s)
\]

\[
T(s) = K_I a(s)
\]

![Fig-3 Block diagram of armature controlled dc motor](image)
The transfer function of dc motor speed with respect to the input voltage can be written as follows

\[ G(s) = \frac{\omega(s)}{V(s)} = \frac{\frac{Kt}{(Ra+2La)(Js+R)+KbRt}}{} \]  

(15)

Armature controlled dc motor are preferred over field controlled system. For small size motor field control is advantageous because only a low power servo amplifier is required while the armature current which is not large can be supplied from an expensive constant current amplifier. For large size motor it is on the whole cheaper to use armature control scheme. Further in armature controlled motor, back emf contributes additional damping over and above that provided by load friction. The combination of proportional, integral and derivative control action is called PID action control and the controller is called three action controllers. Here the proportional part of the control action repeats the change of error and derivative part of the control action adds an increment of output so that proportional plus derivative action is shifted ahead in time. The integral part adds a further increment of output proportional to the area under the deviation line. The combination of proportional, integral and derivative action may be made in any sequence as shown.

IV. MATLAB REPRESENTATION AND SYSTEM RESPONSE:
Transfer function obtain in equation (15) can be simulate on MATLAB by using practical controller parameter (Kd, Ki and Kp) and DC motor parameter as shown in table -1 and table -2.

**Controller Parameters:** In PID controller there are some parameter (Proportional Gain, Derivative Gain, Filter Coefficient, Integral Gain) by varying these parameter response can be change (stability, error, rise time etc. can be control).

**Table -1 Controller Parameters**

<table>
<thead>
<tr>
<th>Controller Parameters</th>
<th>Tuned Gains Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proportional Gain</td>
<td>100</td>
</tr>
<tr>
<td>Derivative Gain</td>
<td>100</td>
</tr>
<tr>
<td>Filter Coefficient</td>
<td>100</td>
</tr>
<tr>
<td>Integral Gain</td>
<td>1</td>
</tr>
</tbody>
</table>

**DC motor Parameters:** Fig. -2 represent electric circuit diagram of dc motor which consist some practical parameter like Armature resistance (Ra), Armature Coil Inductance (La), Equivalent Coefficient of friction of motor shaft & load (B) etc. The performance of DC motor (speed of dc motor, Torque of dc motor, current drawn by dc motor etc) can be control by controlling these parameter. Here we are considering practical value of DC motor parameter for better operation of system that given in table-2.

**Table-2 DC motor Parameters**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Armature resistance (Ra)</td>
<td>0.5</td>
<td>Ohm</td>
</tr>
<tr>
<td>Armature Coil Inductance (La)</td>
<td>1.8*10^{-4}</td>
<td>H</td>
</tr>
<tr>
<td>Armature Torque Constant (Kt)</td>
<td>2.83*10^{-2}</td>
<td>Nm/A</td>
</tr>
<tr>
<td>Back emf constant (K)</td>
<td>2.83*10^{-2}</td>
<td>Vs/rad</td>
</tr>
<tr>
<td>Motor Armature Inertia (J)</td>
<td>20.3</td>
<td>Kgm²</td>
</tr>
</tbody>
</table>

**Equivalent Coefficient of friction of motor shaft & load (B) | 4 | M**
CONCLUSION:
From above experimental results we conclude that kp) will have the effect of reducing the rise time and will reduce; but never eliminate the steady-state error, an integral control (ki) will have the effect of eliminating the steady-state error, but it may make the transient response worse. A derivative control (kd) will have the effect of increasing the stability of the system. Here we have used PID controller with suitable controller parameter as shown in table -2 and response of dc motor drown in Fig-6 which stable and having constant speed 35 rps at (t= 4 sec).

REFERENCES: