

Application of First- Order Linear Equation Market Balance

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ABSTRACT

If we consider economic variables as a continuous function of time, then we will encounter with relations which we have to use differential equations to solve them. If we consider the collection of relations of economic variables that are matched in accordance with the conditions, this collection of relations is called an economic model. models are two types, fixed models and variable models, and fixed models are related to equilibrium. In these models, the variables are independent of time, and when it comes to equilibrium, it does not change anymore, for example, if (p) is supposed the price of a commodity that the function of (p) is the amount of demand (d) and supply (s) in a fixed period, then we have that:

$$d = f(p)$$

$$s = g(p)$$

The above links are a fixed system of economic model.

If the price of many goods is focused, this price is constantly in changing. Sometimes it can be considered a continuous function of time, and the balance of demand and supply is also a continuous function of time, in this case, moreover the demand is a function of its price, it is the function of price changes as well, because if the price is predicted to be added or reduced in the future, it will be effective in terms of supply and demand; therefore, the demand and supply equation is as follow:

$$\begin{cases} d(t) = f[p(t), p'(t)] \\ s(t) = g[p(t), p'(t)] \end{cases}$$

The above is a fixed model. The purpose of this study is to study the importance of the differential equation and its use in economics.

As the result of this article I found that the relationship of differential equations with economics has been mostly closed and expanded, and solution of many issues in economics depends on formation and solving of differential equations.

KEYWORDS: first order linear equation, fixed models, variable models, and market balance

INTRODUCTION

Differential equations are applied to most of the economic functions. These equations are used in determining the conditions for the changeable stability for the balance of economic breakdowns and the tracking of time paths under various macroeconomic conditions. If growth rates are a supposed function, economists are able to determine the slightly function by using differential equations. Also, if a point is calculated, the demand function can be calculated, differential equations are used for calculating investment functions, as well as calculation of total cost and total cost functions from final cost functions and final income. In this research paper, the linear equation of the first order in the market equilibrium is investigated.

OBJECTIVES OF THIS RESEARCH

The main purpose of this research paper is to obtain market equilibrium by a linear first order differential equation.

Methodology:

A descriptive research project is used to focus and identify the effects of differential equations on economics and on human life and the dimensions of society. In advance and completion of this research, books, scientific journals and Internet sites have been used.

Literatures review:

The beginning of the differential equations is the seventeenth century and it is the time when Newton-Leibniz and Bernoulli succeeded in solving several differential equations of the first and second degrees, which arise from geometry and mechanic. These initial discoveries, which their beginning was (1690), apparently gave rise to the idea that the answer to all the differential equations based on the geometric and physical theorem can be expressed in terms of the elementary functions, orientation with the differential calculus and integrals. Therefore, most of the elementary

tasks in innovative ways to solve differential equations were by primary methods of addition, subtraction, multiplication, division, and analysis, with an infinite number of factors depending on the functions, differential calculus, and integral. There were several particular methods accidentally designed, such as the decoding of variables and the use of factors of integral before the end of the seventeenth century.

In the 18th century, more principled procedures were introduced by Euler, Lagrange and Laplace. It quickly appeared that relatively less differential equations could be solved by primary methods. Mathematicians have gradually found that attempting to discover methods for solving all differential equations is vain. Instead, the question is raised in this section that does a differential equation have an answer or not, and if it does, then the attempt is to find the properties of the answer is more effective than the differential equation. In this case, mathematicians found differential equations as new sources of functions.

The massive progress of physics in the last two centuries should be borne in mind by the theory of differential equations. This theory, which consists of ordinary and partial differential equations, is a branch of mathematical analysis, which is closely related to physics. Differential equations in the mid-18th century formed the basis of theoretical physics. Equations in the middle of the century were the most attractive part of this theory. D'Alambert introduced vibrating string and got the first partial differential equations, which is then modeled as the main subject of his work. (porkazimi, 2009)

Then Euler was interested in this equation and he subtilized the unique conditions of the answer. These conditions were resulted the physical concept of the theorem. Euler's articles found the way to find solutions to boundary value problems in the form of trigonometric sequences. This method was later used by Bernoulli in vibrating string, and introduced a wider range of permissible functions in setting the initial conditions. The methods of D'Alambert, Euler, and Bernoulli lead to a long discussion of the effectiveness of the techniques, and then Lagrange and Laplace entered the debate.

Euler in his works has addressed other partial differential equations with complete differential equations, he developed the theory of partial differential equations and then he was identified as the innovator of partial differential equations theory. The trigonometric sequences method was used to obtain answers to quaternary issues by Fourier, which "completed it in the heat conduction equation to the application".

Fourier presented several expanded articles on this issue, among which heat-analytical theory is of particular importance. The use of trigonometric sequences in the heat conduction theory created a new topic of mathematical analysis, called the theory of Fourier sequences.

Partial differential equations came to the other part of physics in which Laplace obtained the potential for interaction between two masses in the equation which is now called the Laplace equation. Because of the electrostatic phenomena and the theory of magnetism also appear, at the beginning of the 19th century, the general theory of potentials was innovated by Green Goss and Pawson.

These results led to the construction of partial differential equations that have a direct relationship with the boundary value problems. This topic was at the height of the nineteenth century and the beginning of the twentieth century, with the main directors of Kochi, Riemann, Poincare, Piker, Holmgren, Had Amar, Garza, and Wizard. The geometric nature of the answers to the partial differential equations, in particular the characteristic theory, opened up another way in this theory.

In the last few decades, new methods have been devised that stand by functional analysis, distribution theory, and generalized functions, and have been greatly works related to these issues accomplished by Schauder and Leray. This vital and useful theory is now the area of the most important mathematical research, and every new attractive matter emerges and grow in it.

Recently, the works and writings of some famous scientists and professors are also seen in the field of differential equations in different parts, but these investigations and writings are not sufficient due to the greatness of the discussion of differential equations, especially in the application of ordinary differential equations First, there has not been much research in economics now.

I hope that this article, which has been written in spite of a series of constraints, can introduce the first-order ordinary differential equations in economic sand reflects the practical importance of the first-order linear differential equations as good as for dear instructors and students.

Stable and unstable balance detection:

One of the conditions for stable balance is its steady state. It means, if for any reason the deviation from balance is achieved, effective forces to operations will lead the market, the amount and the price to balance. For example, in a condition that supply has positive slope and demand has negative slope (typical slope of supply and demand), if we reduce the price for any reason that there is a tendency to return to the initial state, then the balance is stable.

The balance is unstable when moving from the balance point leads to the entry of forces in the market that diverges us from the balance point. If the price is dropped for any reason and with increasing supply, in order to sell the product, due to the increase in supply, the decline in prices should continue to decline.

So, momentarily, we get away from the balance, this is an unstable balance. If the supply and demand curves are consistent, the balance is low or neutral, it means, if we lose the state of balance, there is no factor that causes a distant or near-balance.

Use of first-order linear differential equation in market balance

Demand function $Q_d = c + bp$ and supply function

$Q_s = g + hp$ are supposed to consider a function of time.

We suppose that the rate of price changes in the market $\frac{dp}{dt}$ is being Positive linear function of demand

addition $Q_d - Q_s$, the price of balance equals to $\bar{p} = \frac{c-g}{h-b}$,

as $\frac{dp}{dt} = m(Q_d - Q_s)$ the stability conditions of price change in the market (the conditions that when tendsto infinity, $p(t)$ is tended to p) can be calculated as follow:

$$\frac{dp}{dt} = m(Q_d - Q_s)$$

$$\frac{dp}{dt} = m[(c + bp) - (g + hp)] = m(c + bp - g - hp)$$

The above equation has become the form of a first-order linear differential equation, as we are properly familiar with the methods of its solving from differential equations, so it is calculated as follow:

$$\frac{dp}{dt} = m(h - b)p - m(c - g)$$

$$\frac{dp}{dt} + m(h - b)p = m(c - g)$$

$$v = m(h - b)$$

$$z = m(c - g)$$

We know the general solution form of the first-order linear differential equation that:

$$p(t) = e^{-\int v dt} \left(A + \int z e^{\int v dt} dt \right) = e^{-vt} \left(A + \int z e^{vt} dt \right) = e^{-vt} \left(A + \frac{z e^{vt}}{v} \right)$$

$$p(t) = A e^{-vt} + \frac{z}{v}$$

if $t = 0$, the equation take the following shape:

$$p(t) = \left[p(0) + \frac{z}{v} \right] e^{-vt} + \frac{z}{v} t = 0$$

$$\Rightarrow p(0) = A + \frac{z}{v} \Rightarrow A = p(0) - \frac{z}{v}$$

By laying down $\begin{cases} v = m(h - b) \\ z = m(c - g) \end{cases}$

The following link is achieved:

$$\lim_{p \rightarrow \infty} p(t) = p(e) = \frac{c - g}{h - b} \Rightarrow p(t) = \left[p(0) - \frac{c - g}{h - b} \right] e^{-m(h - b)t} + \frac{c - g}{h - b}$$

ecause m is a constnt amount and is bigger than zero, when t approaches to infinity, only when $h - b > 0$, the first right limit approaches to zero, so $p(t)$ approaches to p. for normal states where the demand has a negative slope $b < 0$ and the supply has a positive slope $h > 0$, the changeable stable conditions is obtained.

The markets that the slope of the demand functions are positive or the slope of supply functions are negative, when $h > 0$ are changeably stable as well. (porkazimi, 2009)

Example 1: Whenever the demand equation is $D = 80 - 4p$ and the supply equation is $S = 2p - 10$ find the Market Balance and suppose that $p_0 = 18$ and $q_0 = 8$ find wetherthe balance is stable or not?

Solution: as we know, the balance point is equal to Supply equation = demand equation

$$2p - 10 = 80 - 4p$$

$$q_e = 20 \quad p_e = 15,$$

and based on $\begin{cases} v = m(h - b) \\ z = m(c - g) \end{cases}$ we solve the following equation.

$$\frac{dp}{dt} + m(h - b)p = m(c - g)$$

$$v = m(2 + 4)$$

$$z = m(80 + 10)$$

$$p(t) = A e^{-6mt} + 15 \quad p(t) = A e^{-6mt} + \frac{90m}{6m}$$

Because the demand has a negative slope $b < 0$ means that $b = -4$ and the supply has a has a positive slope $h > 0$ means that $h = 2$. Therefore, we can achieve that the changeable stability conditions is obtained. (Edward, 1994)

Discussion

The first-order linear differential equation can be used in different parts of the economics, so that in the first step, using the guided differential equation, then we can solve it by using the first-order linear differential equation solution.

In solving these issues, we can use replacements for ease of work, and in other ways, the first change can be reached .

The first-order linear differential equation arises from the facts that we face in the social processes with such concepts and theories that you are required to establish relationships between dependent and free or non-dependent (independent) changes in the form of mathematical and snobbisms, In some states, there is no possibility of the relationship between functions and variables directly and it is even unlikely, but it can be easily defined between its functions and its variables and the derivatives of the desired functions from different order of the snobbisms and the exact mathematical. formulas, so that the formula in total concepts and rules of higher mathematics are referred to as differential equations.

Conclusion

As the result of this article I found that the relationship of differential equations with economics has been mostly closed and expanded, and solution of many issues in economics depends on formation and solving of differential equations, and also I realized that evaluating the first-order linear differential equations in economicis a mathematical phenomenon and the first-order linear differential equations are important in physically changing and principles of economics and in market balance. Needs for recognizing the principles, concepts, laws and use of differential equations come from those truths that in social practical processes we usually confront with those concepts and ideas that imply to study and formulate the relationship between the market balance and stable balances. I also found that in some states, formulating the direct relationship between market balance and stable balance is impossible and even it is unlikely, but easily we can define and formulate the relationship between market balance and stable balance by a mathematical formulating that this mathematical formulating is generally called differential equations.

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