Influence of Penstock Outlet Diameter and Flat Blade Lateral Twist Angle on the Performance of A Simplified Pico Hydropower System

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ABSTRACT

A study to investigate the influence of penstock outlet and the flat blade lateral twist angle on the performance of an existing Pico-hydro system was undertaken. Five penstock reduced from 76.2 mm to 15, 17.5, 20, 22.5 and 25 mm diameters at the outlet and a runner with adjustable flat blades were fabricated from mild steel sheet. For each of the penstock outlets, five blade twist angles of 50, 55, 60, 75 and 90° were tested and the turbine and alternator speed measured with tachometer. The initial and final levels of water in the overhead tank as well as the periods of tests were also measured. The data collected was used to compute the flow rate and power for each set. A maximum computed power of 5600 W was obtained with the 25 mm penstock outlet in conjunction with the blade twist angle of 75°. Also, the maximum speed 1180 rpm of the alternator shaft was obtained for a penstock outlet diameter of about 20.25 mm at the same twist angle of 75°. These results imply that for the system potentially could generate appreciable power using flat blades with the penstock outlets and blade twist angles in the ranges > 20 mm and ≥ 60° respectively. Considering the simplicity of the flat blade configuration, the results indicate good promise for providing relatively cheap, clean and convenient domestic power with further work on the system.

Keywords: Penstock outlet, Flat blades, Lateral twist angle, Turbine speed, Alternator speed, domestic power

I. INTRODUCTION

Energy plays the most vital role in the economic growth, progress, and development, as well as poverty eradication and security of any nation. Uninterrupted energy supply is a vital issue for all countries today. Future economic growth crucially depends on the long-term availability of energy from sources that are affordable, accessible, sustainable and environmentally friendly [1 – 3]. Security, climate change, and public health are closely interrelated with energy [4 – 6]. Energy is an important factor in all the sectors of any country's economy. The standard of living of a given country can be directly related to the per capita energy consumption. The per capita energy consumption is a measure of the per capita income as well as a measure of the prosperity of a nation [7 – 9]. Energy supports the provision of basic needs fuels productive activities including agriculture, commerce, manufacturing, industry, and mining. On the other hand, a lack of access to energy contributes to poverty and deprivation and can contribute to the economic decline [10 – 12]. Energy and poverty reduction are not only closely connected with each other, but also with the socioeconomic development, which involves productivity, income growth, education, and health...
Presently, developing nations globally are suffering from disruptions of energy supply in a situation termed energy crisis. Energy crisis implies a situation in which a nation suffers from disruption of energy supply usually accompanied by rapidly increasing energy price and power interruption that threatens both economic and national security. The situation poses serious questions of sustainability, security of supply, and related changes in climate [16 – 19].

Reliance on the fossil fuels, which are finite, for current global energy needs is over 80%. Understandably, this is causing some fear with devastating consequences for the global economy and quality of life [20, 21]. Ultimately, the near-unlimited supply potential of renewable energy sources should ensure that the world does not fall short of its energy needs. The security of global energy supplies continues to be problematic. Today, oil and gas reserves are in the hands of a small group of nations, several of which are considered politically unstable or have testy relationships with large consuming countries. About 80% the world’s proven oil reserves are located in just three regions in Africa, Russia and the Caspian Basin and the Persian Gulf, with more than half of the world’s remaining proven gas reserves existing in just three countries: Russia, Iran, and Qatar. Concerns over energy security are prompting policymakers to seek independence from foreign sources of energy [22]. In Europe, for instance, new coal-fired power stations are back on the political agenda, partly because Russia is no longer seen as a reliable supplier of gas. In the US, home-grown biofuels have been promoted by successive administrations as an alternative to Middle Eastern oil imports, despite being more expensive. It is envisaged that the more governments can extract themselves from the dependence on foreign energy resources, the greater the likelihood of being energy secured. Also, concerns about global warming primarily as a resulting from the burning of fossil fuels for energy are here. Though some sections of the globe are playing politics with it, the scientific evidence to support this assertion has become increasingly compelling in recent years. Hence, there is a need for urgent and concerted action by all nations to prevent ecological degradation on a massive scale with the attendant fallouts. This can be achieved by switching attention to alternative energy sources such as hydropower [23 – 25].

Nigeria is not left out of the current wave of energy crises. Nigeria is one of the most populated countries in Africa but only about 40% of the people are connected to the energy grid. According to [26], the people who actually have power experience difficulties around 60% of the time and that persistent blackout cripple the industrial sector. Lack of electricity also causes problems for agriculture. Most irrigation lines are run by electricity, so when the power is cut out then the crop yield decreases [27]. Nigeria’s energy grid is arguably in crisis due to lack of development. The key to making a more reliable energy sector is to find and use renewable energy resources, rather than simply relying on the country’s non-renewable resources [28, 29].

Water appears to be the best renewable source of energy because a small-scale hydropower is one of the most cost-effective and reliable energy technologies to be considered for providing clean electricity [30, 31]. Hydropower is a renewable, economic, and environmentally benign source of energy. Hydropower stations have inherent abilities for instantaneous starting, stopping, load variations and so on, helping to improve the reliability of power systems. Hydro stations are also the best choice for meeting peak demand. The generation cost is not only inflation free but reduces with time and hydroelectric projects have long useful life extending over 50 years and help in conserving scarce and environmentally unfriendly fossil fuels [32 – 34]. Furthermore, they open avenues for development of remote and backward areas. It has been reported that hydropower throughout the world provides around 17% of electricity from the currently installed capacity as well as the ones under construction, making it by far the most important renewable energy for electrical power production. Hydropower production is expected to increase significantly over the next century. Hydropower has remained the renewable source of energy that contributes most to electricity generation. The total estimated annual power generation from hydropower presently has surpassed 3,618 TWh/y [35 – 38].

In Nigeria, hydropower currently accounts for more 29% of the total electrical power supply. The hydropower station at Kainji has an installed capacity is 836 MW with provisions for expansion to 1156 MW. The one at Jebba has an installed capacity of 540 MW. It has been estimated since the 1990s that a total capacity of about 4,650 MW exists for Rivers Kaduna,
Benue and Cross River at Shiroro, Makurdi and Ikom respectively with. Only the Shiroro site has been exploited till date. Estimates for the rivers on the Mambila Plateau are put at 2,330 MW. The overall hydropower resource potentially exploitable in Nigeria is in excess of 11,000 MW. The foregoing assessment is for large hydro schemes which have predominantly been the class of schemes in use prior to the oil crisis of 1973 and still remain so though the current Government is taking definite steps to diversify to renewable sources [39 – 45].

Hydropower schemes. Micro- and Pico-hydro technologies are used in developing countries to provide electricity to isolated communities where the electricity grid is not available, whereas mini-hydro tends to be grid connected [53 – 59]. Micro- and Pico-hydro can scheme design can be approached on a per household basis or at village level often involving local materials and labor whereas mini-hydro schemes require traditional engineering approaches unlike mini-hydro. Also, mini-hydro schemes will usually require an access road to be built for construction materials and heavy electro-mechanical equipment to be delivered to the site, whereas most micro-hydro schemes can be built with purely manual labor in more remote locations. Also, since electricity from micro- and Pico-hydro schemes can be supplied directly to households, there is no large grid to control the frequency and voltage of the supply, hence only a local load controller is necessary. For Pico hydro, the turbine/generator set can be bought as a modular, off-the-shelf unit, unlike the equipment for larger schemes (micro-hydro and upwards) where the specific requirements are taken into consideration in the design/selection of the turbine/generator [60 – 62]. There have been growing interests in research and development into Pico-hydro systems especially in Asian countries. This could have largely been as a result of the need to diversify from fossil fuels, the necessity of off-grid options for better access to rural communities and the natural obstacle which the topography imposes against large scale developments. Implementation is highly advanced leading to significant commercial activities. Discussions are intense and include many different perspectives, from personal experiences highlighting the needs of indigenous people, to the requirements of power intensive industries. Priorities are focused on the need for strategic approaches, and a broader engagement when it comes to energy and water planning. There is also growing interest in the use of pumps as turbines (PATs). This basically involves the use of centrifugal pumps working in the reverse mode. More attention is also currently being given to the pumped-storage hydropower system to supply high peak demands by moving water between reservoirs at different elevations [63 – 66].

The low electrification rate as well as the unsteady nature of power supply in Nigeria hinders the fight against poverty and the development of the country. Apart from the environmental and health hazards posed by fossil fuels which hitherto are the major
energy source, there are numerous other challenges such as scarcity, cost and prospect of depletion. This calls for a shift of attention to alternative sources of energy, of which hydro power is one. This has motivated the development of a simple Pico hydropower system. The system has the capacity of mitigating against the shortcomings of conventional hydropower systems while conferring control to the end user and reducing the risks of vulnerability to sabotage and other insurgent activities [26, 29, 42, 67]. The penstock and runner design significantly affects the performance of a Pico hydropower system. This study seeks to find the optimum penstock outlet and the flat blade lateral twist angle of a simplified Pico hydro turbine, in order to improve its performance and provide additional data in this area of study. The general principle revolves around its simplicity and adaptability to locations where there is no naturally flowing water. Moreover, its scalability for better performance has already being proved from previous aspects that have been reported [68 – 71].

II. MATERIALS AND METHOD

The materials for this work were selected based on previous aspects of this work [68 – 71]. Mild steel was used for the entire turbine construction, and was chosen for the reasons of its good weldability, machinability, ductility and toughness, and in addition to the availability of the material at an affordable cost compared to other metals. The runner comprised of a circular hub with 10 flat blades equally spaced around the hub with a blade to hub ratio of about 0.55 as used by [72]. The hub and blades were fabricated from 2 mm and 1.5 mm thick mild steel sheet respectively. The blades were structurally made different from the ones used in earlier aspects of the work by being adjustable so that the test can be carried out at different blade angles. Figure 1 shows the assemble runner with the adjustable blades.

The penstock outlets were made from 1.5 mm mild steel sheet and had outlet diameters of 15, 17.5, 20, 22.5 and 25 mm. Figure 2 shows the various diameter penstock outlets.

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Following the complete fabrication of the runner, it was then clamped to the shaft flange with three M10 bolts and mounted in between two bearings and seals on the already existing turbine casing and cover to allow free spinning of the shaft and prevent leakages in the turbine [70]. The bearings were lubricated to minimize friction. The turbine casing cover was then secured in position with M14 and M13 bolts and the turbine pulley of diameter 605 mm was mounted to the end of the shaft.

The experimental set up in this study consisted of a pump rated 2 Hp with a flow capacity of 50 l/min and a locally fabricated turbine connected in a closed loop with the help of PVC piping as penstock, a 2000 liters overhead tank and a 3000 liters underground reservoir. Figure 3 shows a picture of the entire system. The suction pipe of the pump draws water from the underground reservoir to the overhead tank to create a head. Water is released from the overhead tank through the penstock and flows through tapered outlet into the turbine casing. The flow through the turbine is regulated using a gate valve installed before entry to the penstock. The water jet strikes the blades transferring its kinetic energy to the shaft and causing the rotary motion of the rotor. The turbine shaft transmits the torque to a 50 mm diameter pulley fixed to the alternator through a toothed v-belt drive in a step up ratio of 12:1, causing the rotary motion of the alternator shaft, thereby generating a voltage. The water in the turbine casing is directed through an outlet port into an underground reservoir from where it is re-cycled to the overhead tank by the pump.
The adjustable blades of the turbine were adjusted laterally to angles of 50, 55, 60, 75 and 90° one after the other, and for each angle, the penstock outlet was varied from 15 to 25 mm in steps of 2.5 mm. In each case, the rotational speeds of the turbine and alternator shafts were measured using a DT-2268 Contact Type Digital Tachometer. The water levels in the underground and overhead reservoirs before and after each operation were measured using a calibrated dip stick and the duration measured using a stopwatch. The difference in water level for the underground reservoir was used to compute the flow rate $Q$ using the expression:

$$Q = \frac{\Delta V}{t}$$  \hspace{1cm} (1)

Where $Q$ is the flow rate in the penstock in m$^3$/s, $\Delta V$ is the change in volume of water in the overhead tank in m$^3$ and $t$ is the time of flow in seconds.

The gross head available was approximately determined by adding the total height of the penstock (7 m) to the depth of water in the underground reservoir.

The major losses $h_f$ were computed using equation 2 defined by [73] as

$$h_f = \frac{6.87L}{D^{1.165}} \left( \frac{V}{C} \right)^{1.85}$$  \hspace{1cm} (2)

Where $V$ is the flow velocity, $D$ is the penstock diameter; $L$ is pipe length and $C$ the Hazen-Williams coefficient. For plastic pipes $C$ is between 135 and 140 while for steel pipes it is 150.

The minor losses were computed using 3 defined by [74] as

$$H_{minor} = \frac{V^2}{2g} \sum K_i$$  \hspace{1cm} (3)

Where $K_i$ = Coefficients for pipe shape geometry and area contraction.

The net head available was computed by subtracting the total losses from the gross head for each operation. The fluid power was computed using 4.

$$P_f = \tau \omega$$  \hspace{1cm} (4)

Where $\tau$ = torque produced and $\omega$ = angular velocity.

The ideal or expected values of the alternator shaft speed were computed using 5, where $N_T$, $N_A$ are the respective turbine and alternator shaft speeds, and $D_T$, $D_A$ the corresponding pulley diameters.

$$\frac{N_A}{N_T} = \frac{D_T}{D_A}$$  \hspace{1cm} (5)

These ideal values were then compared with the actual experimental ones and a percentage error computed based on their differences. The alternator shaft speed, computed power and the computed percentage errors were then analyzed for variation at 95% confidence interval based on the twist angles and different penstock outlet diameters.

Figure 4 shows a plot of the alternator shaft speed ($N_A$) against blade lateral twist angle ($\theta$). It is observed that the speed (rpm) of the alternator for 25 mm, 20 mm and 17.5 mm penstock outlet increases at different rates as the blade angle increases from 50° to about 78° and then decreases at 90°. The increase of blade angle increases the tangential (turbine driving) component of the hydraulic force which also increases the drag force. Thus at 78°, the drag force balances the driving force, and since hydraulic head is reducing,
the speed of the alternator shaft decreases. At 50° its speed (105.2 rpm) is higher than that of the 17.5 mm nozzle but lower than the 25 mm nozzle while the 20 mm nozzle at around 75° yields the highest speed than the rest of the nozzles. Beyond 75° the effective surface area of blade becomes too large so that increase in drag forces results, and thus decreases the speed of the turbine. For 22.5 mm the speed at 50 degrees is highest (480 rpm) but decreases at 52° and then increases to a maximum value of 1015 rpm at 72°. At 60° blade angle the alternator speed is same for 20 mm, 22.5 mm and 25 mm nozzles respectively. This suggests that this angle could be the turning point for this arrangement of the system beyond which the performance deteriorates. In summary 20 mm nozzle at a blade twist angle of 78° shows the best performance while 15 mm nozzle at 50° shows the poorest performance. Generally, the effective jet creation and sufficient blade surface area play a very crucial role in the system performance as with conventional hydropower systems [75 - 80].

![Fig. 4: Variation of Alternator Shaft Speed with Blade Lateral Twist Angle](image)

Figure 4 shows the variation of alternator shaft speed with blade lateral twist angle. For 22.5 mm nozzle the speed at 50 degrees is highest (480 rpm) but decreases at 52° and then increases to a maximum value of 1015 rpm at 72°. At 60° blade angle the alternator speed is same for 20 mm, 22.5 mm and 25 mm nozzles respectively. This suggests that this angle could be the turning point for this arrangement of the system beyond which the performance deteriorates. In summary 20 mm nozzle at a blade twist angle of 78° shows the best performance while 15 mm nozzle at 50° shows the poorest performance. Generally, the effective jet creation and sufficient blade surface area play a very crucial role in the system performance as with conventional hydropower systems [75 - 80].

Figure 5 shows the plot of N_A against nozzle diameter. The graph shows that the optimum performance of turbine with the flat blades was obtained with the blade at about 77.5° and the nozzle diameter of 23.8 mm. As can be seen, the speed of 1200 rpm was achieved with the 23.8 mm nozzle. At 61° blade angle, the performance of the 20 mm, 22.5 mm and 25 mm nozzles was similar as it can be seen in the graph. Beyond 77.5° blade angle drag force coupled with reduction in head reduces the speed of the turbine. The poorest performance was obtained with 15 mm nozzle and blade angle at 50°.

![Fig. 5: Variation of Alternator Shaft Speed with Penstock Outlet Diameters](image)

Figure 5 shows the plot of N_A against nozzle diameter. The graph shows that the optimum performance of turbine with the flat blades was obtained with the blade at about 77.5° and the nozzle diameter of 23.8 mm. As can be seen, the speed of 1200 rpm was achieved with the 23.8 mm nozzle. At 61° blade angle, the performance of the 20 mm, 22.5 mm and 25 mm nozzles was similar as it can be seen in the graph. Beyond 77.5° blade angle drag force coupled with reduction in head reduces the speed of the turbine. The poorest performance was obtained with 15 mm nozzle and blade angle at 50°.

Figure 6 shows a graph of the computed power against blade angle. At 50° blade angle, 25 mm nozzle gives the highest power with the power decreasing with decrease in blade angle. The power for the two nozzles (20 mm and 17.5 mm) increased steadily till 65° blade angle and then fell. The 25 mm nozzle gives the highest value of power (6000 W) at 83° blade angle, followed by 22.5 mm nozzle which gave the value of 3700 W at 70° blade angle. At 77° degrees blade angle the two graphs for 20 mm and 17.5 mm nozzle intersect at 250 W. Also at 88° blade angle the 17.5 mm and 22.5 mm nozzle gave the same power output of 2600 W. The results
corroborate the fact that larger penstock outlet supports higher flow rates which translates to better performance in terms of power generated [81 - 89].

Figure 7 shows a graph of computed power against penstock diameter. The initial power for 25 mm nozzle was the highest and decreased with decrease in the penstock nozzle diameter. The highest value of power which is 5600 W was obtained with 23 mm nozzle, followed by the 22.5 mm nozzle which produced 3600 W, 3000 W were obtained with 25 mm penstock nozzle. The least value of power was obtained with the 17.5 mm nozzle. At 23 mm nozzle, 20 mm and 17.5 mm nozzles gave the same value of power which is 600 W.

Tables 1 to 3 show the results of the analysis of variance of the alternator shaft speed, computed power and error percent based on the difference between the actual and ideal alternator shaft speeds. At 95% confidence interval, table 1 shows that the alternator shaft speed is statistically significantly affected by the penstock outlet (columns) and the blade lateral twist angle (rows). Table 2 also indicates a similar conclusion with regards to the computed power which is to be expected because the power computation involved the alternator shaft speed. However, the variation of the computed power with the penstock outlet was more significant than that with the twist angle. This is probably because the penstock outlet directly affects the generation of the water jet before impact with the blades. Table 3 however, indicates that the variation of the departure of the experimental values of the alternator shaft speed from the ideal values using 5 with the penstock outlets and the blades twist angles were not statistically significant at 95% confidence interval. This could partly be because this departure most likely resulted from the structural and mechanical errors with the turbine rather than the twist angle or the penstock outlet.
Table 1: ANOVA of Alternator Speed for the Various Penstock Outlets and Twist Angles

<table>
<thead>
<tr>
<th>Source of Variation</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>F</th>
<th>P-value</th>
<th>F crit</th>
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<td>2.34E-06</td>
<td>3.006917</td>
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<tr>
<td>Error</td>
<td>297898.3</td>
<td>16</td>
<td>18618.64</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Total</td>
<td>2945642</td>
<td>24</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Table 2: ANOVA of Computed Power for the Various Penstock Outlets and Twist Angles

<table>
<thead>
<tr>
<th>Source of Variation</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>F</th>
<th>P-value</th>
<th>F crit</th>
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</thead>
<tbody>
<tr>
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<td>1021515</td>
<td>4.799053</td>
<td>0.009782</td>
<td>3.006917</td>
</tr>
<tr>
<td>Columns</td>
<td>55722471</td>
<td>4</td>
<td>13930618</td>
<td>65.44567</td>
<td>1.03E-09</td>
<td>3.006917</td>
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<tr>
<td>Error</td>
<td>3405724</td>
<td>16</td>
<td>212857.7</td>
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<tr>
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</tbody>
</table>

Table 3: ANOVA for Percentage Errors in Alternator speeds from the ideal values

<table>
<thead>
<tr>
<th>Source of Variation</th>
<th>SS</th>
<th>df</th>
<th>MS</th>
<th>F</th>
<th>P-value</th>
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<td>Rows</td>
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<td>179.0804</td>
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An attempt was made to relate the trends of these loss percentages of the alternator shaft speed from the ideal values. The mean computed loss percent values were plotted against the blade twist angle and the penstock outlet diameters as shown in figures 8 and 9 respectively. The trends in the figures are generally similar which appears to buttress the fact that this parameters are not directly responsible for the loss in alternator shaft speed. However, the figures show an indication of that the ranges of $22.5 \geq Penstock\ Outlet \geq 17.5$ and $75^\circ > Lateral\ Twist\ Angle > 55^\circ$ produced the lower loss percentages. These can further strengthen the earlier assertion that for good performance the selection of penstock outlet diameter and lateral twist angle of flat blades for this system should be around these ranges for any further work with this combination of parameters.

![Fig. 8: Variation of Alternator Speed Loss Percent with Blade Lateral Twist Angle](image-url)
CONCLUSION

The results obtained indicate that the performance of the system is affected by the penstock outlet diameter and the flat blade lateral twist angle. The ranges of these parameters suitable for this system are penstock outlet diameter \( \geq 20 \text{ mm} \) and blade twist angle \( > 60^\circ \). Therefore, this is the combination with the best potential for use with the Pico hydro system with possibility for scaling to suit specific requirements of the performance of the system.

From the findings of this investigation, the following recommendations are made for further aspects of the work:

1. Turbine casings used should have adequate provision for the runner not to run through the water so that drag forces on it can be minimized.
2. Standard turbine housing with built in nozzle mounts which allows for large scale adjustments and accommodates different runner sizes should be constructed, as even a small jet misalignments can have a significant negative effects on turbine efficiency.
3. Larger diameter pipes should be used in transferring water to the overhead tank to sustain the flow cycle though it may be at the expense of justifiable higher cost.
4. Lighter metals such as aluminum should be used in fabricating the runners and blades to reduce inertia and probably improve turbine performance.
5. Better awareness and technical understanding of the potentials of the Pico-hydro system needs to be fostered at the local and regional levels in Nigeria so that rural electrification projects can be implemented more effectively.

REFERENCES


Master degree thesis presented to the department of Mechanical Engineering, Oregon State University.


